

Stochastic wind speed modelling including daily wind patterns based on real data

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1. Introduction – Motivation

- UK has ambitious **renewable energy targets** (2020) → **increased wind penetration** → system operation and balancing problems → need for more detailed wind modelling [1]
- **Wind speed has stochastic behaviour** → **driven by natural sources** [1,2]
 - ◊ **Cyclicity** over period of 24 hours (**diurnal cycle**) and longer
 - ◊ **Noisy short-term** stochastic variations (not analytically tractable)
- **How to model this?** → Stochastic Differential Equations (SDEs) → Existing approaches [2-4]
 - ◊ Do not account for **daily cycles**
 - ◊ Lack of **empirical fitting** and validation of the model's parameters
 - ◊ **Weibull distribution** cannot capture **daily cycles and temporal correlation**

2. The SDE model

Wind speed modelled with Ornstein-Uhlenbeck Geometric Brownian Motion in continuous time [2]

$$\ln X(t) = Y(t) + f(t) \quad (1)$$

$$dY(t) = -\kappa Y(t) dt + \sigma dW \quad (2)$$

- $f(t)$ the **deterministic diurnal cycle** based on log-wind speed data
- $Y(t)$ the **mean-reverting stochastic** component of Ornstein-Uhlenbeck type
- κ, σ, dW the **mean reversion parameter, volatility and Wiener process**
 - Probability Density Function (PDF) of wind speed → **log-normal PDF**
 - PDF of wind power **not Gaussian** → wind power **cannot** be modelled with an **O-U GBM model**
 - **Annual cycle** neglected → short term decisions needed in power system operation and balancing

3. Parametric estimation

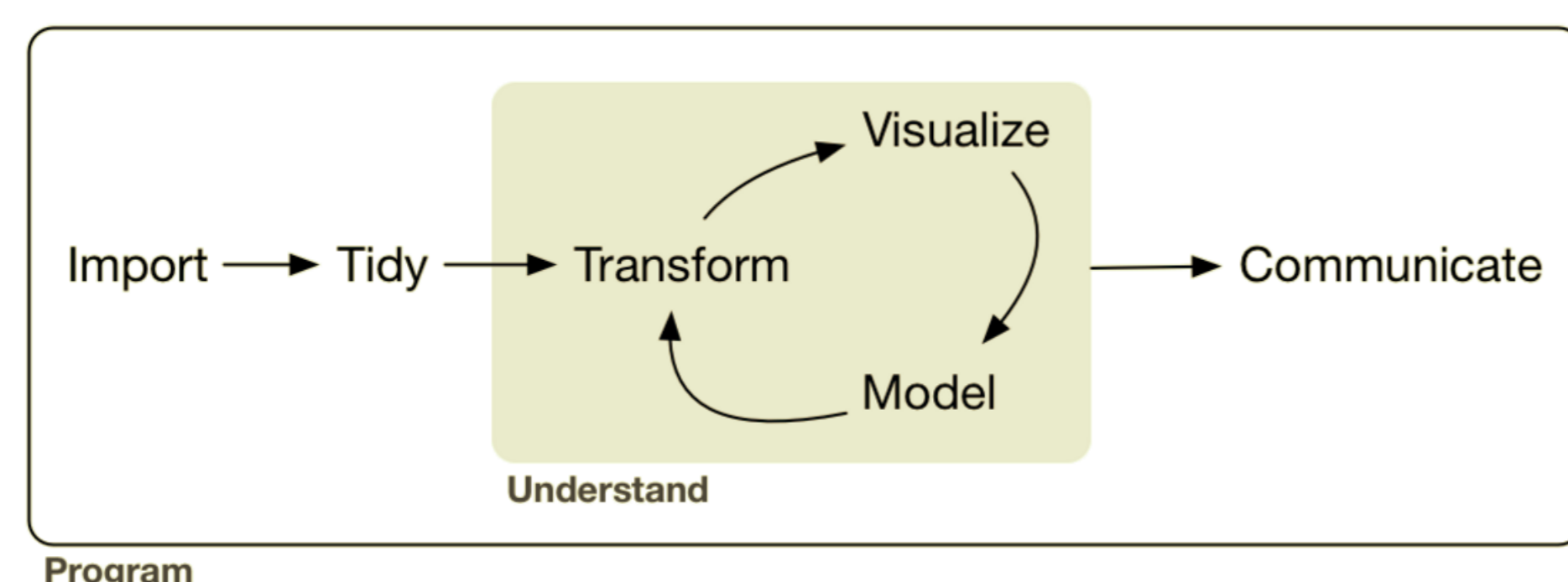


Figure 1: General steps of analysing the wind speed dataset [5]

Import – Tidy

Import data into a data frame → Real data used – collected from Spanish wind farm [6]

- ◊ 10-minute resolution
- ◊ summer season (June-July-August) of years 2010-2016 selected to compute **average summer daily cycle**
- ◊ specific month of June 2016 selected for fitting the **stochastic component**

Tidy the dataset → Columns: variables (date, wind speed, wind power) – Rows: observations [5]

- ◊ Fix date to specific format **year-month-date**
- ◊ Change wind speed observations **from factor type to numeric**
- ◊ No **missing values** observed – remove **outliers** (4 very high unusual wind speed values)

Transform – Visualise

Initial wind speed time series – PDF (Figs 2-3) – **summary statistics** (Table 1)

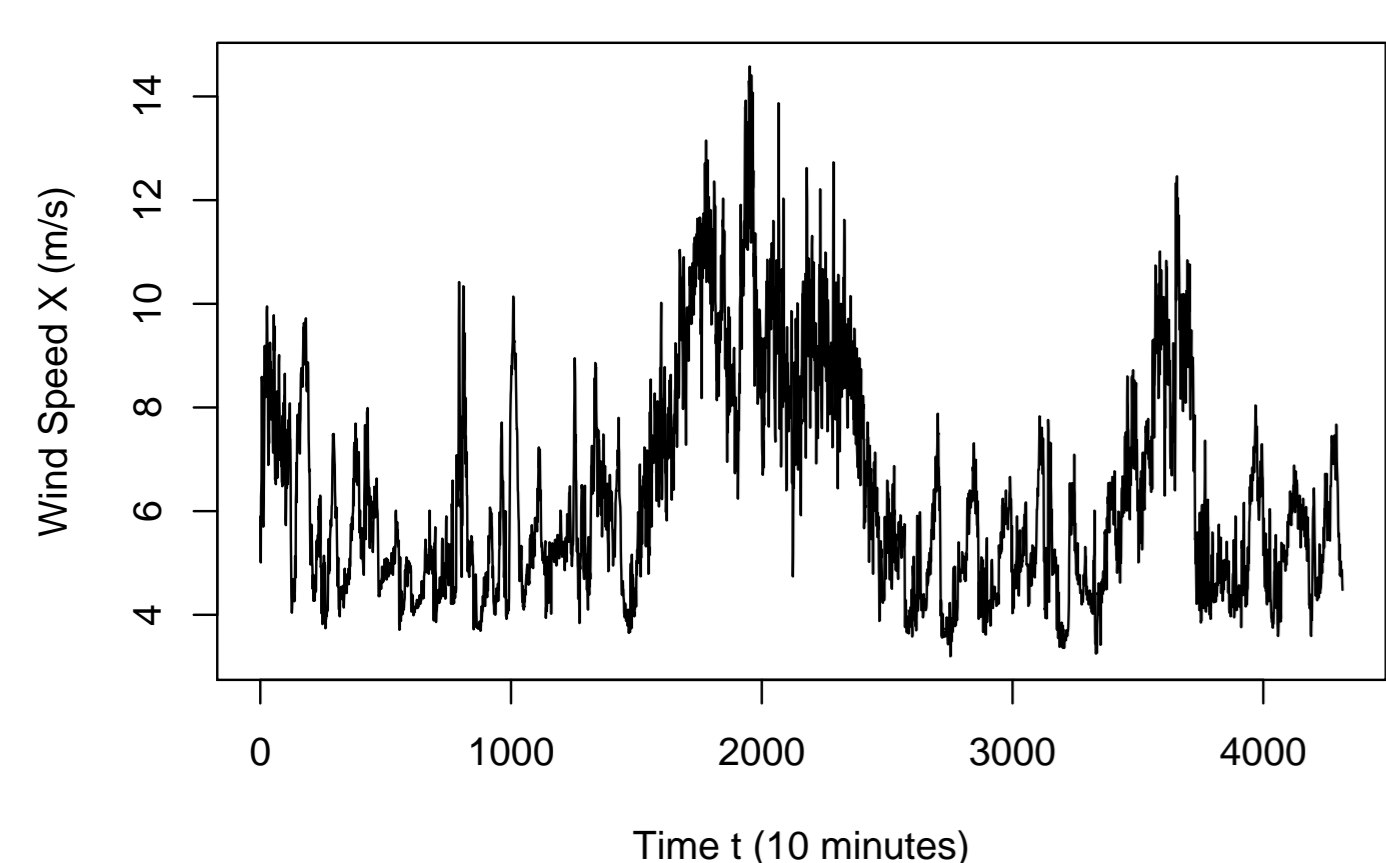


Figure 2: Wind speed time series with time resolution of 10 minutes for June 2016 [6]

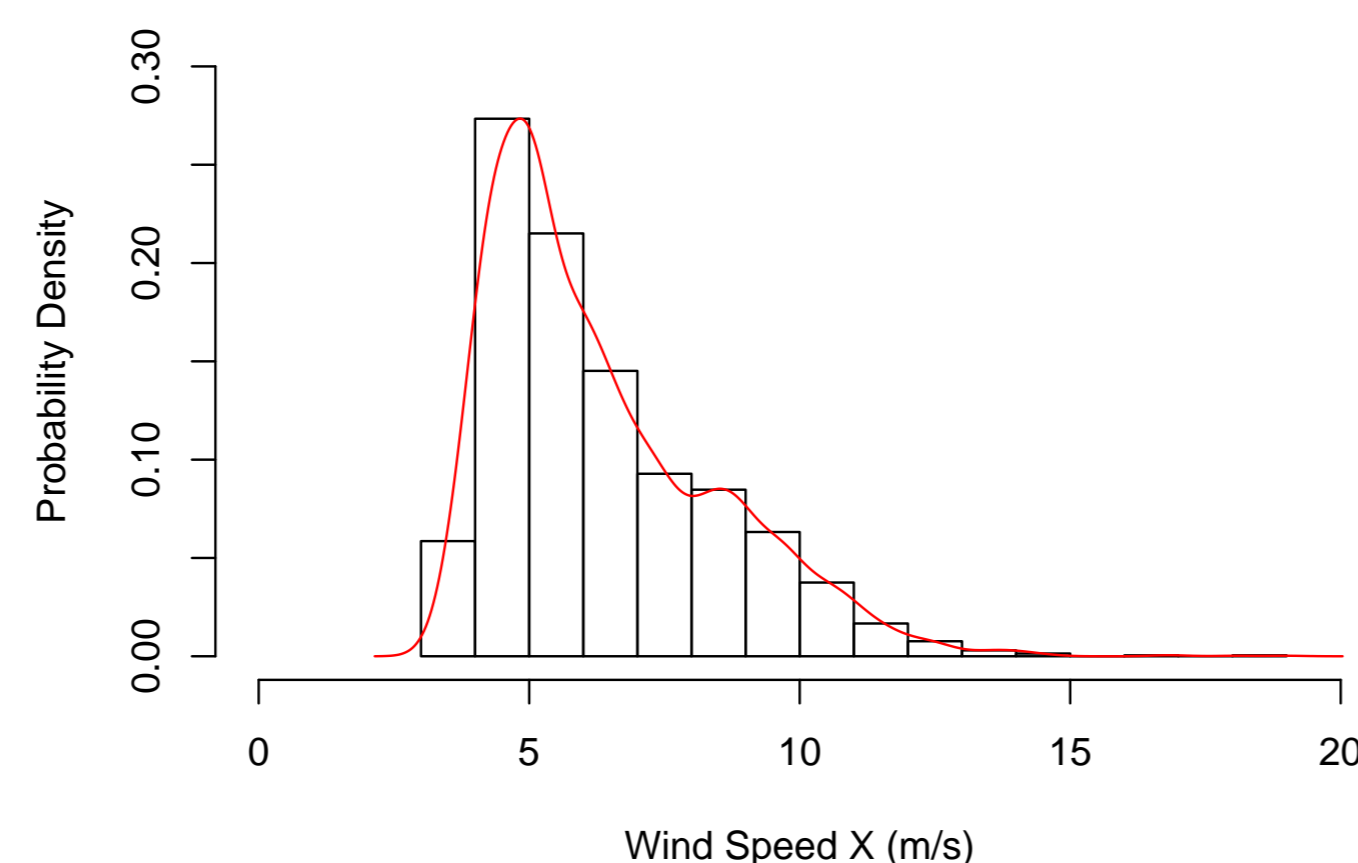


Figure 3: Histogram (black) of empirical wind speed data and kernel PDF (red) of wind speed for June 2016 [6]

Table 1: Main statistical characteristics of the wind speed time series for June 2016 (max, min, mean and sd in m/s)

	Time	X-min	X-max	X-mean	X-sd
	10-min	3.2	18.98	6.34	2.1

Computed daily averages → existing daily pattern with higher wind speeds during the evening (Fig. 4)
Average summer daily cycle → ensure adequate accuracy (fitted with Fourier series, Fig. 5)

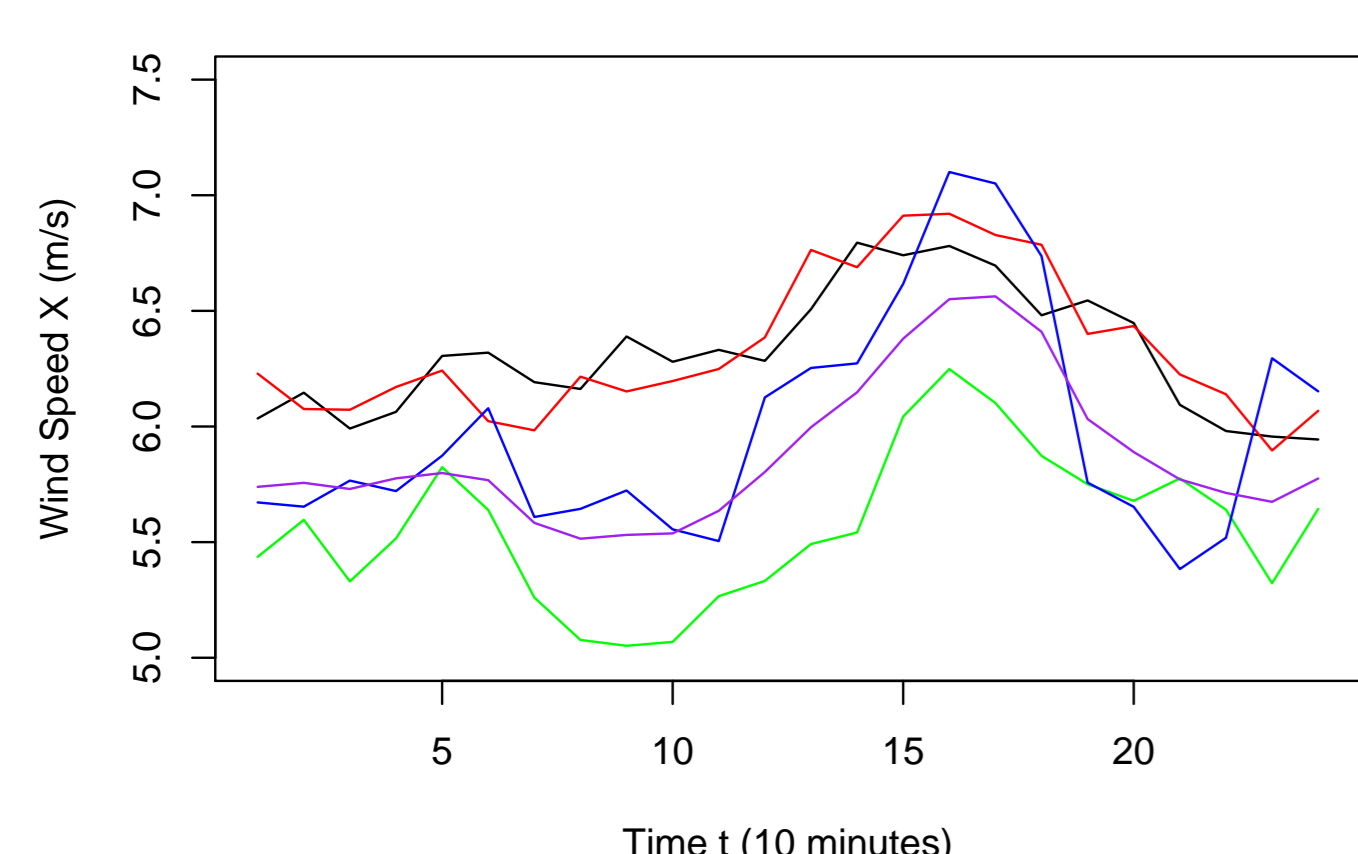


Figure 4: Average daily cycles: June 2014 (blue), June 2015 (green), June 2016 (red), June 2017 (black), average daily cycle for the whole summer season (purple) [6]

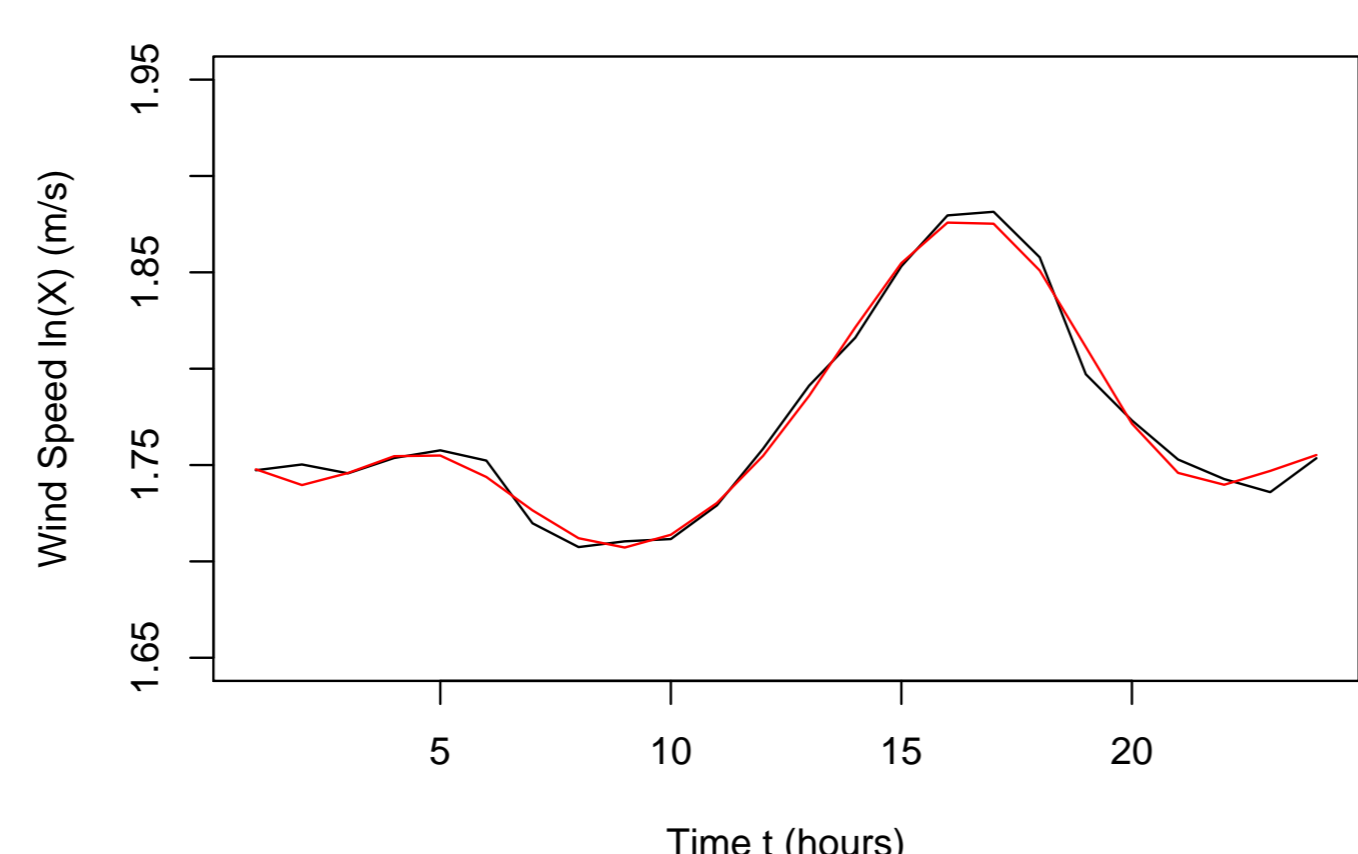


Figure 5: Average summer daily wind speed profile (black) and fitted daily cycle (red) with a Fourier series model (with frequencies of $w, 2w$ and $3w$) for log-wind speed [6]

Empirical Validation of SDE Model

- ◊ Calculate **logarithms** of initial wind speed time series
- ◊ Remove the average summer daily cycle presented in Fig. 5 [1,3-5]
- ◊ Estimate κ and σ with maximum likelihood estimators [3,5] (Table 2)
- ◊ **Residual analysis** → residuals resemble white noise [1,3] (Figs 6-7)

Table 2: Parameter values for the stochastic component of the wind speed model

Parameter	Values	Standard error
$\hat{\kappa}$	0.0368	0.0041
$\hat{\sigma}$	0.0819	0.00088

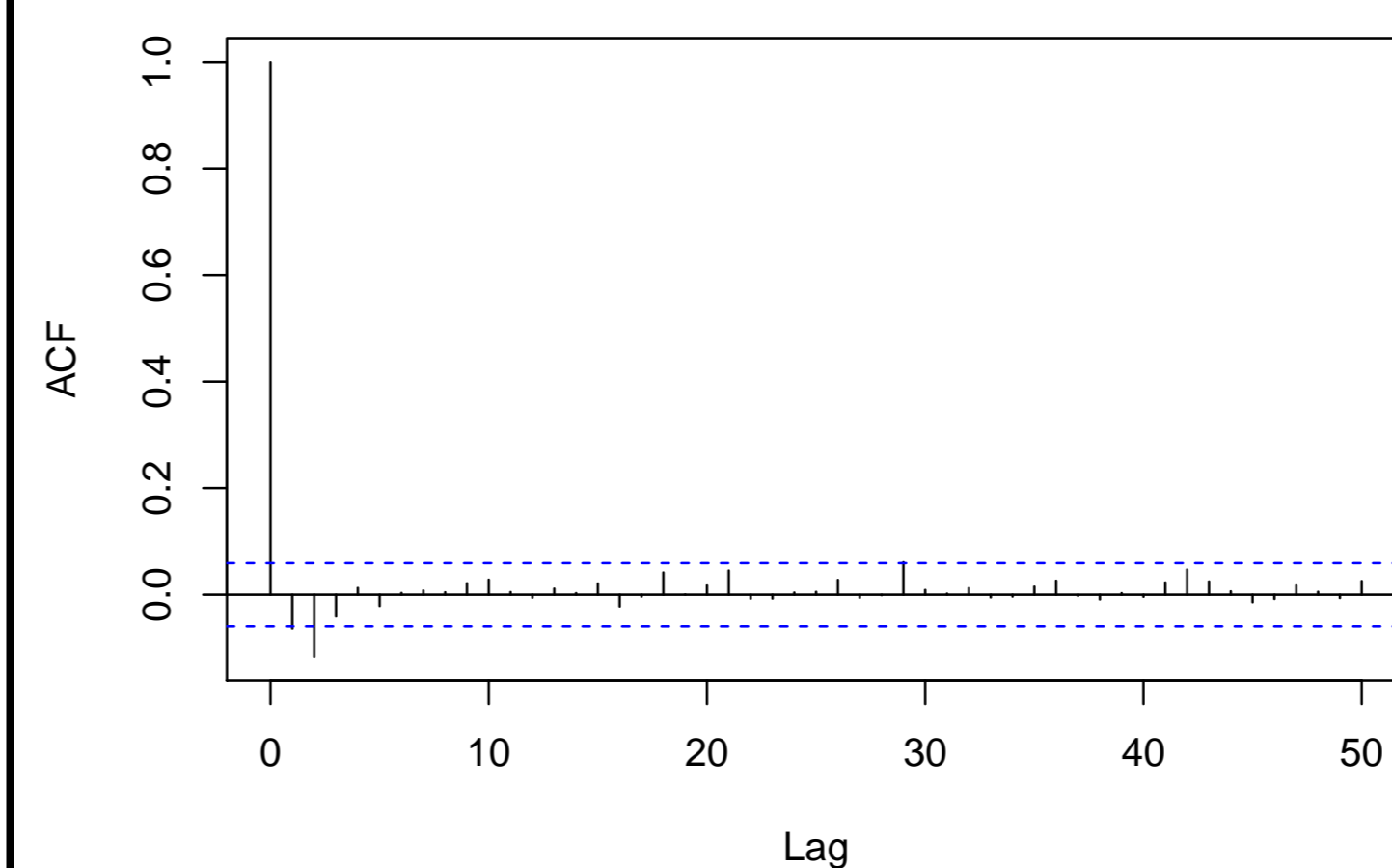


Figure 6: ACF of the residuals for the de-trended log-wind speed data for the Spanish wind farm (95% confidence interval)

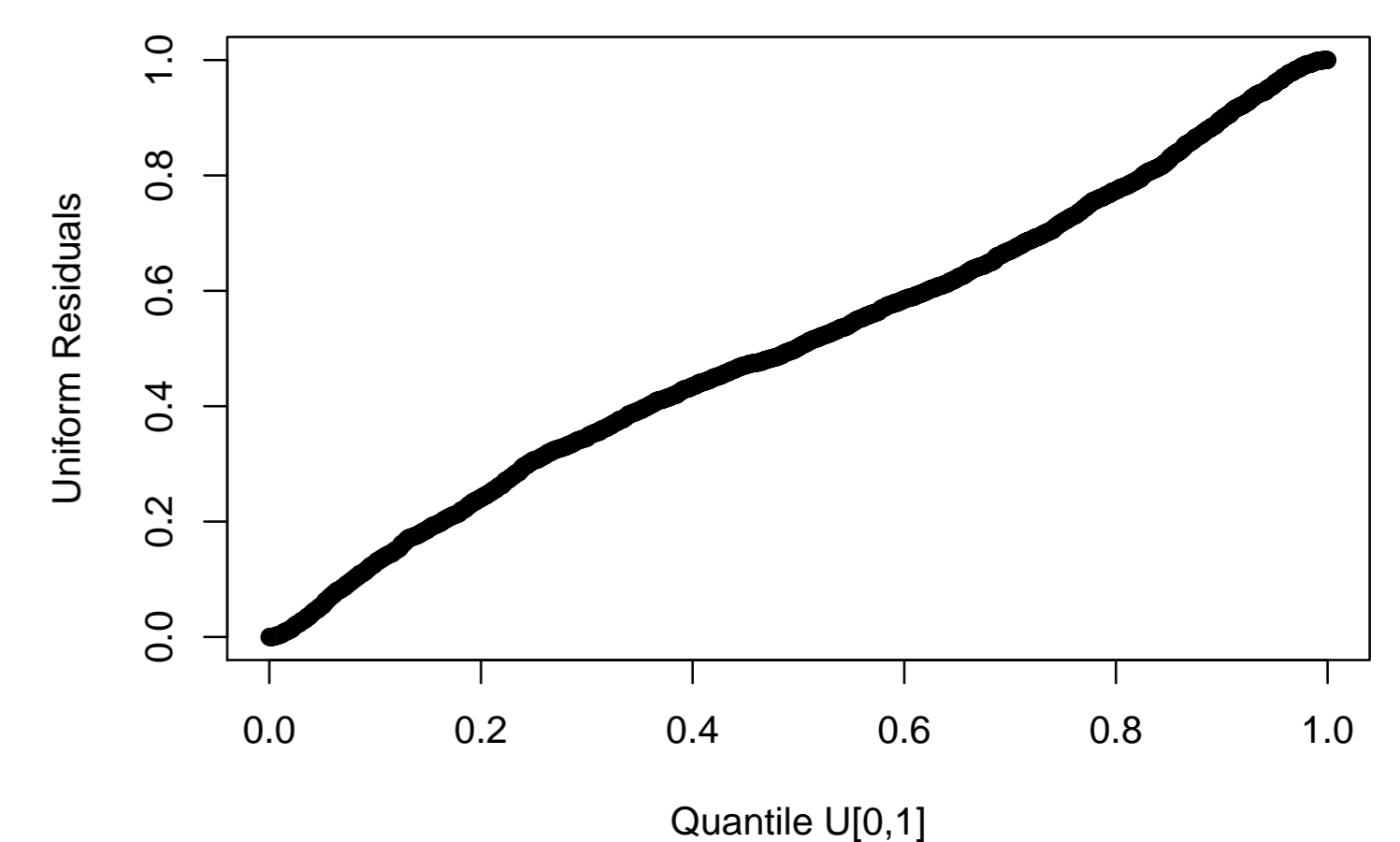


Figure 7: Uniform residues quantile – quantile graph of the de-trended log-wind speed data

4. Communicate Results

◊ SDE of Eqs (1)-(2) solved numerically with **Milstein scheme**

◊ **Parameters used:** $\kappa = 0.0368, \sigma = 0.0819, n = 4320, \delta t = 0.167$, fitted average summer daily cycle, $f(t)$, first observation of the initial wind speed time series used as starting point, random variable drawn from the $N(0, 1)$ distribution multiplied by $\sqrt{\delta t}$

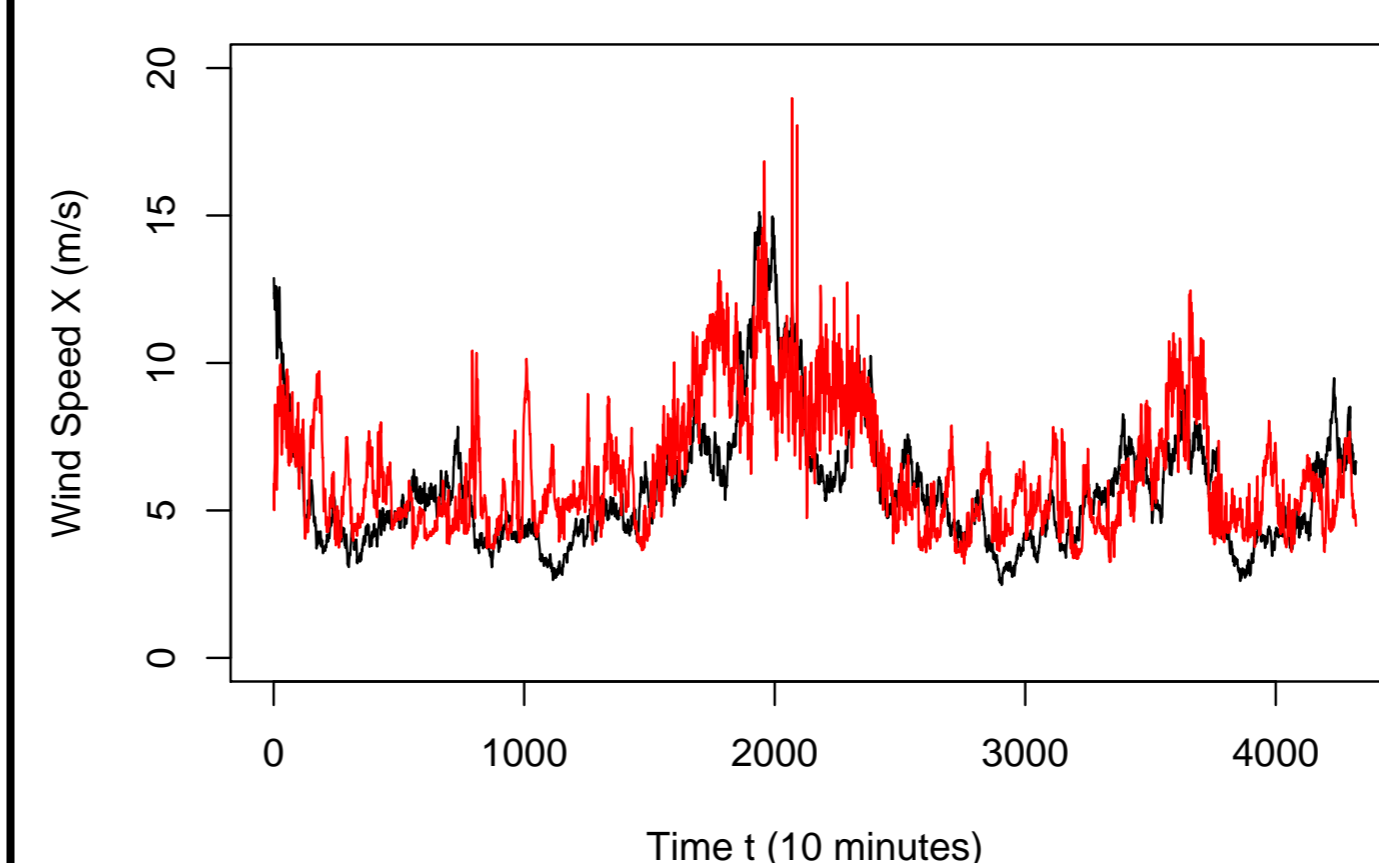


Figure 8: Simulated (black) and empirical (red) wind speed time series for the 10-minute data for June 2016

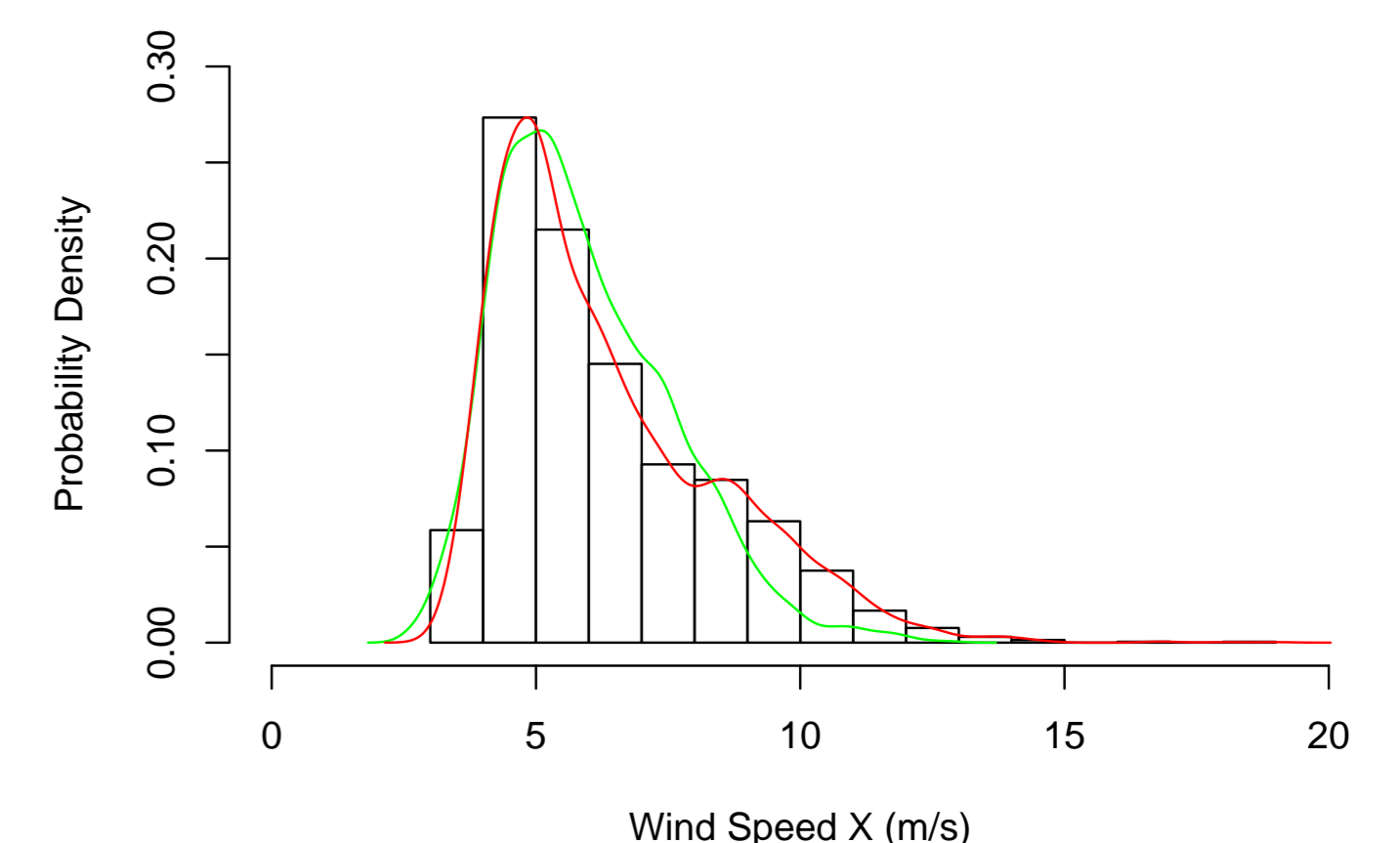


Figure 9: Empirical (red) and simulated (green) PDFs with histogram (black) for the 10-minute data for June 2016

1. **Simulated wind speed** follows empirical time series closely – they **change similarly over time** and remain **within the same limits** as also shown from histogram and PDFs (Figs 8-9)
2. **Correlation** between empirical and simulated wind speed: 0.61, **Root Mean Square Error** between PDFs: 0.073
3. **Mean-reverting nature of the model** → simulated wind speed starts at higher value than the long-term mean but it reverts back to the mean daily cycle

5. Conclusion

- ◊ Proposed model **fitted and validated with real data**
- ◊ Proposed model **adequately represents wind speed variations** in continuous time
- ◊ Proposed model easily **adjusted to other time resolution** from that of the given data
- ◊ Proposed model can be used for various applications – **optimal energy storage or system balancing**

Future work:

- ◊ **Different data sets** → different daily cycles and examine their impact on the stochastic wind model
- ◊ **Wind power curve** → compute and analyse wind power output

6. References

1. C. Hill, D. McMillan, R. Bell, and D. Infield, "Application of auto-regressive models to uk wind speed data for power system impact studies," *IEEE Transactions on Sustainable Energy*, vol. 3, no. 1, pp. 134141, Jan. 2012.
2. P. Johnson, S. Howell and P. Duck, "PDE methods for stochastic dynamic optimisation: an application to wind power generation with energy storage", *Philosophical Transactions A*, vol. 375, no. 2100, Jul. 2017.
3. H. Verdejo, A. Awerkin, E. Saavedra, W. Kiemann, L. Vargas, "Stochastic modeling to represent wind power generation and demand in electric power system based on real data," *Applied Energy*, vol. 173, pp. 283-295, Apr. 2016.
4. O. Magnus, P. Magnus, S. Lennart, "Modeling real-time balancing power demands in wind power systems using stochastic differential equations," *Electric Power Systems Research*, vol. 80, pp. 966-974, Feb. 2010.
5. W. Hadley and G. Grolemond, "R for data science," 2016.
6. "Real-time Wind Data," *Sotavento 2017*, [online], Available: <http://www.sotaventogalicia.com/en/real-time-data/historical>, [Accessed: 23 Oct-2017].

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